

**Topics in Empirical Economics****Linear regression model (OLS and IV)**

**A.** Use the dataset “ols.dta” and consider the following population model

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + u$$

with  $cov(x_1, u) = 0$  and  $cov(x_2, u) = 0$ .

1. Use the Frisch-Waugh theorem to estimate  $\beta_1$  and compare your result with the  $\hat{\beta}_1$  that you get from a multiple regression.
2. Are the effects of  $x_1$  and  $x_2$  comparable? If not, can you make them comparable?

**B.** Use the dataset “iv.dta” and suppose we are only interested in the effect of  $x_1$ . Consider the following population model

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + u.$$

$z$  is a potential instrumental variable for  $x_1$ . The following conditions hold jointly:  $cov(x_1, u) \neq 0$ ,  $cov(x_2, u) = 0$  and  $cov(z, u) = 0$ .

1. Is  $z$  a relevant instrument for  $x_1$ ?
2. Use OLS and 2SLS to estimate  $\beta_1$ . Which one gives you a consistent estimate? And why?
3. How can you test the exogeneity of  $x_1$ ?
4. Now, assume we don't observe  $x_2$ . Under what additional assumption is the IV estimate of  $\beta_1$  consistent?